

# Learning Random Walk Models for Inducing Word Dependency

## Distributions

Kristina Toutanova, Christopher Manning, Andrew Ng  
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## Outline

- ★ Markov Chains
- ★ Prepositional Phrase Attachment Problem
- ★ Random Walks



# Markov Chains

- ★ Markov Distribution
  - ★ States  $\mathcal{S}$
  - ★ Initial distribution:  $p_0(S)$  over all  $S \in \mathcal{S}$
  - ★ State transition probabilities:  $p(S_t|S_{t-1})$



# Markov Chains

- ★ Generating a Markov Chain
  - ★ Generate initial state,  $S_0$ , based on  $p_0$
  - ★ Generate remaining states,  $S_t$ , based on transition probabilities
- ★ Stationary distribution (if the limit exists):

$$\pi(s) = \lim_{t \rightarrow \infty} P(S_t = s)$$



# Markov Chains

- ★ How to ensure a stationary distribution?
  - ★ Include probability  $\gamma > 0$  of resetting to initial distribution  $p_0$
  - ★ New state transition distribution:

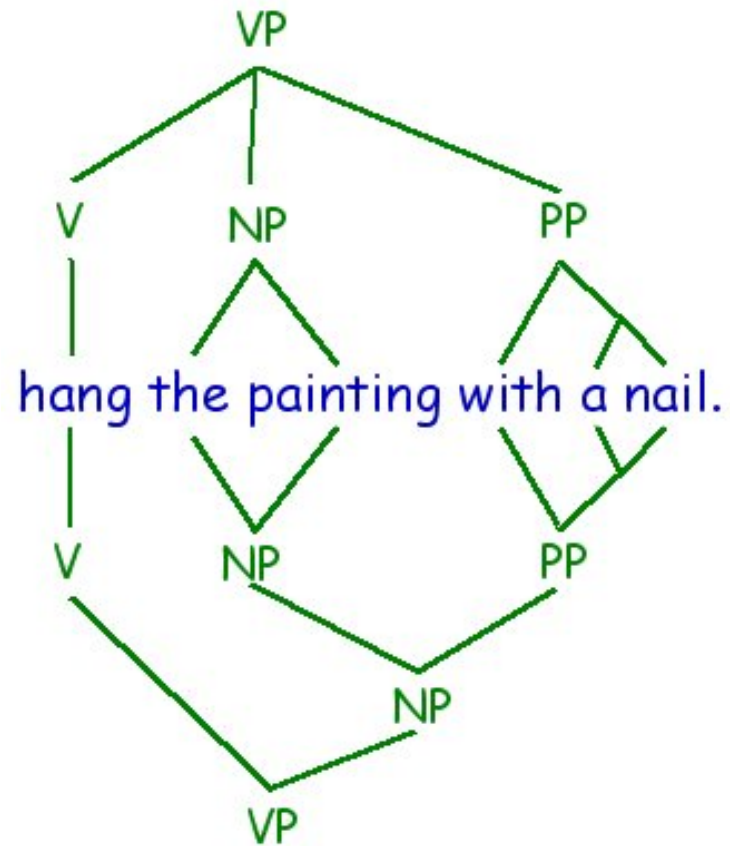
$$p(S_t|S_{t-1}) = \gamma p_0(S_t) + (1 - \gamma) p'(S_t|S_{t-1})$$

- ★ Stationary distribution (can be approximated) becomes:

$$\pi(s) = \gamma \sum_{t=0}^{\infty} (1 - \gamma)^t P(S_t = s)$$



# PP Attachment Problem





## PP Attachment Problem

★  $v$ :hang  $n_1$ :painting  $p$ :with  $n_2$ :nail

★  $P(V, N_1, P, N_2, Att) \Rightarrow P(Att|V, N_1, P, N_2)$

★  $Att = va$  (verb attachment) or  $na$  (noun attachment)

★  $P(v, n_1, p, n_2, va) =$

$$P(p, va)P(v|p, va)P(n_1|p, va, v)P(n_2|p, v, va)$$

★  $P(v, n_1, p, n_2, na) =$

$$P(p, na)P(v|p, na)P(n_1|p, na, v)P(n_2|p, n_1, na)$$



## Random Walks

- ★ But how to generate the probabilities?
  - ★ Random Walks!
- ★  $\mathcal{S} = \mathcal{W} \times \{0, 1\}$ 
  - ★  $\mathcal{W}$  = all words, 0 = head state, 1 = dependent state
  - ★ nail = {nail, 1}, hang = {hang, 0}
- ★  $p_0(\text{verb}, 0) = 1$



## Random Walks

- ★ Separate graphs for each probability distribution (e.g.  $P(N_2|p, v, va)$ )
- ★ Separate transition matrices (graphs) for each  $p$
- ★ "Short" walks away are likely related; "long" walks are not as likely



## Transition types

- ★ Empirical transitions: What was seen in the training set
- ★ Morphology: Words with same root and same marker (nail vs. nails)
- ★ WordNet Synsets: Semantically similar words (nail vs. rivet)

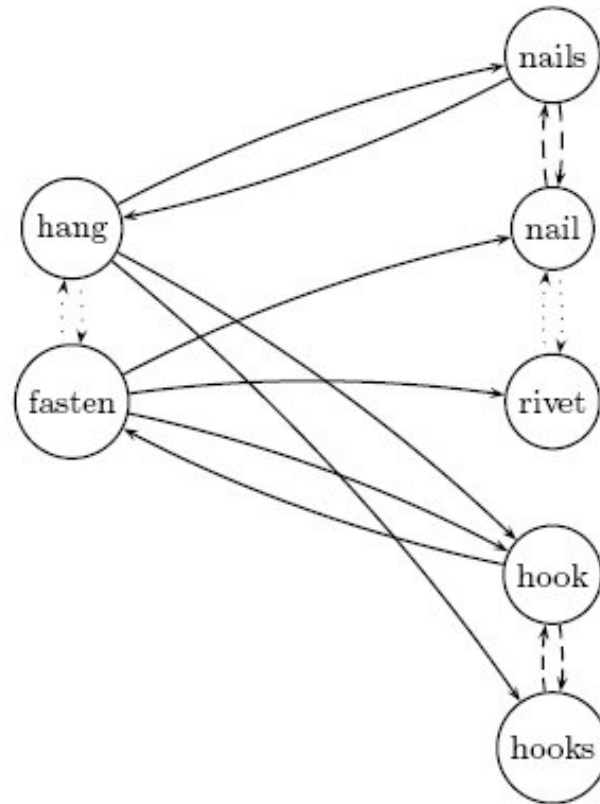


## Transition types

- ★ External Corpus: Similar to empirical transition, but includes noisy data (from a statistical parser)
- ★  $V \rightarrow V$ : Verbs that take similar dependents (hang vs. fasten)
- ★  $N \rightarrow V$ : Nouns with similar heads (nail vs. rivet)



# Random Walks



State space for learning  $P_{with}(n_2, v)$



## Experiments

- ★ Penn Treebank WSJ for training and test set
- ★ BLLIP corpus for noisy data (1.8 million sentences; Charniak parser)
  - ★ 567,582 ambiguous PP tuples extracted
- ★ Run the Markov chain  $d$  time steps (degree)
- ★ Try different types of links



## Results

Model	Degree	Accuracy
Baseline	1	85.86%
Baseline+stem verbs	1	86.02%
Morph Verbs	2,3	86.08%
Morph Verbs and Nouns	2,3	86.18%
Morph & Synonyms	2,3	86.53%
$Sim_{JS_\beta}$	2,3	86.44%
Final	2,3	87.54%

★ Baseline: run chain for one step (linear interpolation)



## Conclusions

- ★ Random walk models provide general framework for similarity based smoothing
- ★ Random walk of step 1 is just linear interpolation (baseline)
- ★ Gives high performance in prepositional phrase attachment
  - ★ Can be applied to other problems as well